

**PROBLEM SET 7, 347, FALL 2005**  
**DUE WEDNESDAY 10/19**

(1) (10 points) Let  $\underline{n}$  denote the set

$$\underline{n} = \{1, \dots, n\}.$$

- (a) Prove (for example by induction) that the power set  $\mathcal{P}(\underline{n})$  of  $\underline{n}$  has  $2^n$  elements.  
(b) Now prove the following formula:

$$2^n = \sum_{k=0}^n \binom{n}{k}$$

(2) (20 points) Read Chapter 5 of the book. Then do questions 5.50, 5.10, 5.13 and 5.23 from the book.